

Visualization 4. Ratios of different quantities with respect to those in corresponding reference systems. (a) r $\delta R$ ratio of radiative rate enhancements at excitation and emission, (b) rcQE ratio of the corrected quantum efficiencies at emission wavelength, (c) rPat total fluorescence enhancement ratio and $\mathrm{r} P_{x} c Q E$ objective function ratio. Lines are to guide eyes and to uncover tendencies of depicted quantities in groups of ( $\mathrm{a}, \mathrm{b}, \mathrm{c}$ ) spherical and ellipsoidal nanoresonators, among them (a) excitation and emission phenomena, and at both wavelengths 4 and 6 color centers separately, (c) $\mathrm{r} P_{\mathrm{x}}$ factor and $\mathrm{r} P_{\mathrm{x}} c Q E$ and for both ratios 4 and 6 color centers separately.

## Colors indicate, when certain quantity is larger in case of

| 4 | 6 |
| :---: | :---: |
| coated | bare |
| spherical | ellipsoidal |

number of emitters
type of nanoresonator
geometry of nanoresonator

| ratio | bare_4 |  | coated_4 |  | bare_6 |  | coated_6 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | spherical | ellipsoidal | spherical | ellipsoidal | spherical | ellipsoidal | spherical | ellipsoidal |
| $\mathrm{rcQE} E_{e m}$ |  |  |  |  |  |  |  |  |
|  | 1.00 | 1.03 | 1.00 | 1.05 | 1.01 | 1.04 | 1.00 | 1.02 |
| $\mathrm{r} \delta R_{\text {ex }}$ |  |  |  |  |  |  |  |  |
|  | 4.00 | 4.00 | 3.98 | 4.00 | 5.99 | 6.00 | 5.98 | 6.01 |
| $P^{N} *_{e x} / P^{1} *_{e x}$ |  |  |  |  |  |  |  |  |
|  | 16.000 | 15.995 | 15.920 | 15.999 | 35.940 | 36.022 | 35.880 | 36.036 |
| $r \delta R_{\text {em }}$ |  |  |  |  |  |  |  |  |
|  | 4.02 | 4.13 | 4.01 | 4.17 | 6.03 | 6.21 | 6.01 | 6.13 |
| $P^{N} *_{e m} / P^{1}{ }^{*}{ }_{e m}$ |  |  |  |  |  |  |  |  |
|  | 16.080 | 16.506 | 16.040 | 16.673 | 36.180 | 37.271 | 36.060 | 36.774 |
| $r P_{x}$ |  |  |  |  |  |  |  |  |
|  | 16.07 | 16.50 | 15.97 | 16.67 | 36.13 | 37.29 | 35.95 | 36.81 |
|  |  |  |  |  |  |  |  |  |
|  | 16.15 | 17.04 | 15.96 | 17.42 | 36.33 | 38.71 | 36.04 | 37.71 |

Table corresponding to Visualization 4. Ratios of different quantities in a coupled system consisting of $N$ collectively oscillating siV color centers and a corresponding reference system consisting of one single SiV color center, which prove the switching into superradiantly enhanced collective states in optimized nanoresonators. $N$ : number of color centers, $\mathrm{rcQE} E_{\mathrm{em}}=c Q E^{\mathrm{N}}{ }_{\mathrm{em}} / c Q E^{1}{ }_{\mathrm{em}}$ : ratio of corrected quantum efficiencies at emission, $\mathrm{r} \delta R_{\mathrm{ex}}=\delta R^{N}{ }_{\mathrm{ex}} / \delta R^{1}{ }_{\text {ex }}$ : ratio of excitation rate enhancements, $P^{N *}{ }_{e x} / P^{1 *}{ }_{\text {ex }}$ : ratio of enhanced powers radiated by a coupled superradiant and a reference system at the excitation wavelength, r $\delta R_{\mathrm{em}}=\delta R^{N}{ }_{\mathrm{em}} / \delta R^{1}{ }_{\mathrm{em}}$ : ratio of emission rate enhancements, $P^{N *}{ }_{\mathrm{em}} / P^{1 *}{ }_{\mathrm{em}}$ : ratio of enhanced powers radiated by a coupled superradiant and a reference system at the emission wavelength, $\mathrm{r} P_{\mathrm{x}}=P_{\mathrm{x}}^{\mathrm{N}} / P_{\mathrm{x}}^{1}$ : ratio of $P_{\mathrm{x}}$ factors, $\mathrm{r} P_{\mathrm{x}}=P_{\mathrm{x}} c Q E^{\mathrm{N}} / P_{\mathrm{x}} c Q E^{1}$ : ratio of objective functions.

